

# Package ‘FARS’

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**Type** Package

**Title** Factor-Augmented Regression Scenarios

**Version** 0.1.0

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**Description** Provides a comprehensive framework in R for modeling and forecasting economic scenarios based on multi-level dynamic factor model. The package enables users to: (i) extract global and block-specific factors using a flexible multilevel factor structure; (ii) compute asymptotically valid confidence regions for the estimated factors, accounting for uncertainty in the factor loadings; (iii) estimate factor-augmented quantile regressions; (iv) recover full predictive densities from these quantile forecasts; and (v) estimate the density when the factors are stressed.

**Depends** R (>= 3.5.0)

**Imports** ggplot2, plotly, sn, nloptr, ellipse, SyScSelection, quantreg, tidy, dplyr, forcats, MASS, reshape2,

**Suggests** devtools, knitr, rmarkdown, openxlsx, readxl, zoo

**VignetteBuilder** knitr

**License** GPL (>= 2)

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compute_fars	<i>Compute Factor Augmented Quantile Regressions and Stressed Quantiles</i>
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### Description

Performs quantile regressions of a dependent variable on MLDFM-extracted factors. Optionally generates quantile forecasts under stressed scenarios using hyperellipsoids.

### Usage

```
compute_fars(
  dep_variable,
  factors,
  h = 1,
  edge = 0.05,
  scenario = NULL,
  min = TRUE
)
```

### Arguments

dep_variable	A numeric vector representing the dependent variable (e.g., GDP growth, inflation).
factors	A matrix of factor estimates from a mldfm model.
h	Integer. Forecast horizon (in time steps) for the quantile regression. Default is 1.
edge	Numeric. Trimming amount applied to the outermost quantiles (default 0.05).
scenario	Optional list of matrices representing a stressed scenario, as returned by create_scenario().
min	Logical. If TRUE (default), implement a stepwise minimization. If FALSE, implement a stepwise maximization.

**Value**

A list containing:

Quantiles Matrix of forecasted quantiles (rows = time, cols = quantile levels).

Scenario\_Quantiles Matrix of stressed scenario quantiles (same format), returned only if scenario is provided.

Coeff Matrix of quantile regression coefficients for each quantile.

Std. Error Matrix of Std. Error for each regression coefficient.

Pvalue Matrix of p-values for each regression coefficient.

**Examples**

```
data <- matrix(rnorm(1000), nrow = 100, ncol = 519)
dep_variable <- rnorm(100) # A numeric vector
block_ind <- c(63, 311, 519) # Defines 3 blocks
r <- c(1, 1, 1, 1, 1, 1, 1) # 2^3 - 1 = 7 nodes
mldfm_result <- mldfm(data, blocks = 3, block_ind = block_ind, r = r)
fars_result <- compute_fars(dep_variable, mldfm_result$Factors, h = 1, edge = 0.05, min = TRUE)
```

---

create_scenario	<i>Create Stressed Scenarios</i>
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---

**Description**

Constructs confidence regions (hyperellipsoids) for the factor space based on a central MLDFM estimate and a set of subsampled estimates. These regions capture estimation uncertainty and are used to simulate stresses scenarios.

**Usage**

```
create_scenario(model, subsamples, data, block_ind, alpha = 0.95)
```

**Arguments**

model	An object of class mldfm, containing the factor estimates.
subsamples	A list of mldfm objects returned from mldfm_subsampling.
data	A numeric matrix or data frame containing the time series data. Rows represent time points; columns represent observed variables.
block_ind	A vector of integers indicating the end index of each block. Must be of length blocks and in increasing order. Required if blocks > 1.
alpha	Numeric. Confidence level (level of stress) for the hyperellipsoid (e.g., 0.95).

**Value**

A list of matrices representing the hyperellipsoid points for each time observation.

**Examples**

```
data <- matrix(rnorm(1000), nrow = 100, ncol = 519)
block_ind <- c(63, 311, 519) # Defines 3 blocks
r <- c(1, 1, 1, 1, 1, 1, 1) # 2^3 - 1 = 7 nodes
mldfm_result <- mldfm(data, blocks = 3, block_ind = block_ind, r = r)
mldfm_subsampling_result <- mldfm_subsampling(data, blocks = 3, block_ind = block_ind, r = r,
n_samples = 100, sample_size = 0.9)
scenario <- create_scenario(mldfm_result, mldfm_subsampling_result, data, block_ind, alpha = 0.95)
```

---

density

---

*Compute Skew-t Densities from Forecasted Quantiles*


---

**Description**

Fits a skew-t distribution to a set of quantile forecasts using linear optimization

**Usage**

```
density(
  quantiles,
  levels = c(0.05, 0.25, 0.5, 0.75, 0.95),
  est_points = 512,
  random_samples = 5000,
  seed = NULL
)
```

**Arguments**

quantiles	A matrix of forecasted quantiles. Each row is a time observation; each column a quantile level.
levels	A numeric vector of the quantile levels corresponding to the columns of the quantile matrix (default: c(0.05, 0.25, 0.50, 0.75, 0.95)).
est_points	Integer. Number of evaluation points for the estimated density (default: 512).
random_samples	Integer. Number of random samples to draw from the fitted skew-t distribution (default: 5000).
seed	Optional integer to set the random seed for reproducibility (default: NULL).

**Value**

An object of class "fars\_density", which is a list containing the following components:

**density** A matrix of estimated densities for each time period (rows) across estimation points (columns).

**distribution** A matrix of random draws from the fitted skew-t distribution for each time period.

**x\_vals** The sequence of evaluation points used to compute the density. Useful for plotting.

**Examples**

```
Quantiles <- matrix(rnorm(500, mean = 0, sd = 1), nrow = 100, ncol = 5)
Levels <- c(0.05, 0.25, 0.5, 0.75, 0.95)
density_result <- density(Quantiles,
                          levels = Levels,
                          est_points = 512,
                          random_samples = 100000,
                          seed = 42)
```

---

mldfm

*Estimate Multilevel Dynamic Factor Model*


---

**Description**

Estimates a multilevel dynamic factor model from time series data. Supports both single-block and hierarchical multi-block structures with customizable factor extraction settings.

**Usage**

```
mldfm(
  data,
  blocks = 1,
  block_ind = NULL,
  r = c(1),
  method = 0,
  tol = 1e-06,
  max_iter = 1000,
  verbose = TRUE
)
```

**Arguments**

**data** A numeric matrix or data frame containing the time series data. Rows represent time points; columns represent observed variables.

**blocks** Integer. Number of blocks into which the data is divided.

block_ind	Integer vector. End column indices for each block. Must be of length blocks and in increasing order.
r	Integer vector of length $2^{\text{blocks}} - 1$ . Specifies the number of factors for each node in the hierarchical structure.
method	Integer. Method used to initialize the factors: 0 for Canonical Correlation Analysis (CCA), 1 for Principal Component Analysis (PCA).
tol	Numeric. The tolerance level for the residual sum of squares (RSS) minimization process. Used as a convergence criterion.
max_iter	Integer. The maximum number of iterations allowed for the RSS minimization process.
verbose	Logical. If TRUE (default), print a summary of the mldfm.

### Value

An object of class mldfm, which is a list containing the following components:

**Factors** Matrix of estimated factors.

**Factors\_hat** Matrix of estimated hat factors.

**Lambda** Matrix of factor loadings.

**Residuals** Matrix of residuals.

**Iterations** Number of iterations before convergence.

**Factors\_list** List of estimated factors for each node.

### Examples

```
data <- matrix(rnorm(1000), nrow = 100, ncol = 519)
block_ind <- c(63, 311, 519) # Defines 3 blocks
r <- c(1, 1, 1, 1, 1, 1, 1) # 2^3 - 1 = 7 nodes
result <- mldfm(data, blocks = 3, block_ind = block_ind, r = r)
summary(result)
```

---

mldfm\_subsampling

*Subsampling Procedure for MLDFM Estimation*

---

### Description

Repeatedly applies the MLDFM estimation to randomly drawn subsamples of the input data.

**Usage**

```
mldfm_subsampling(
  data,
  blocks = 1,
  block_ind = NULL,
  r = c(1),
  method = 0,
  tol = 1e-06,
  max_iter = 1000,
  n_samples = 10,
  sample_size = 0.9,
  seed = NULL
)
```

**Arguments**

<code>data</code>	A numeric matrix or data frame containing the time series data. Rows represent time points; columns represent observed variables.
<code>blocks</code>	Integer. The number of blocks into which the data is divided.
<code>block_ind</code>	A vector of integers indicating the end index of each block. Must be of length <code>blocks</code> and in increasing order. Required if <code>blocks &gt; 1</code> .
<code>r</code>	A vector of integers specifying the number of factors to extract for each node in the block hierarchy. Its length must equal $2^{\text{blocks}} - 1$ , corresponding to all nodes in the hierarchical tree.
<code>method</code>	Integer. The method used to initialize the factors: 0 for Canonical Correlation Analysis (CCA), 1 for Principal Component Analysis (PCA).
<code>tol</code>	Numeric. The tolerance level for the residual sum of squares (RSS) minimization process. Used as a convergence criterion.
<code>max_iter</code>	Integer. The maximum number of iterations allowed for the RSS minimization process.
<code>n_samples</code>	Number of subsamples to generate.
<code>sample_size</code>	Proportion of the original sample to retain (e.g., 0.9 for 90%).
<code>seed</code>	Optional integer. Seed for reproducibility of the subsampling process. If NULL, random draws will differ each run.

**Value**

A list of `mldfm` objects, one for each subsample.

**Examples**

```
data <- matrix(rnorm(1000), nrow = 100, ncol = 519)
block_ind <- c(63, 311, 519) # Defines 3 blocks
r <- c(1, 1, 1, 1, 1, 1, 1) # 2^3 - 1 = 7 nodes
result <- mldfm_subsampling(data, blocks = 3, block_ind = block_ind, r = r,
  n_samples = 100, sample_size = 0.9)
```

---

nl_density	<i>Compute Skew-t Densities from Forecasted Quantiles (Nonlinear Optimization)</i>
------------	--

---

### Description

Fits a skew-t distribution to a set of quantile forecasts using nonlinear optimization

### Usage

```
nl_density(
  quantiles,
  levels = c(0.05, 0.25, 0.5, 0.75, 0.95),
  est_points = 512,
  random_samples = 5000,
  seed = NULL
)
```

### Arguments

quantiles	A matrix of forecasted quantiles. Each row is a time observation; each column a quantile level.
levels	A numeric vector of the quantile levels corresponding to the columns of the quantile matrix (default: c(0.05, 0.25, 0.50, 0.75, 0.95)).
est_points	Integer. Number of evaluation points for the estimated density (default: 512).
random_samples	Integer. Number of random samples to draw from the fitted skew-t distribution (default: 5000).
seed	Optional integer to set the random seed for reproducibility (default: NULL).

### Value

An object of class "fars\_density", which is a list containing the following components:

**density** A matrix of estimated densities for each time period (rows) across estimation points (columns).

**distribution** A matrix of random draws from the fitted skew-t distribution for each time period.

**x\_vals** The sequence of evaluation points used to compute the density. Useful for plotting.



**Examples**

```
Quantiles <- matrix(rnorm(500, mean = 0, sd = 1), nrow = 100, ncol = 5)
Levels <- c(0.05, 0.25, 0.5, 0.75, 0.95)
density_result <- nl_density(Quantiles,
                             levels = Levels,
                             est_points = 512,
                             random_samples = 100000,
                             seed = 42)
```

---

`plot.fars`*Plot Method for fars Object*

---

**Description**

Generates line plots of forecasted quantiles from a FARS object. If a stressed scenario is available, it is plotted in a separate panel.

**Usage**

```
## S3 method for class 'fars'
plot(x, dates = NULL, ...)
```

**Arguments**

<code>x</code>	An object of class <code>fars</code> .
<code>dates</code>	Optional vector of dates (as <code>Date</code> or <code>zoo::yearqtr</code> ) to use for the x-axis. If not provided, a simple index is used.
<code>...</code>	Additional arguments (currently ignored).

**Value**

No return value. Called for plot generation.

---

`plot.fars_density`*Plot method for fars\_density objects*

---

**Description**

Plots the evolution of the estimated density over time as a 3D surface.

**Usage**

```
## S3 method for class 'fars_density'
plot(x, time_index = NULL, ...)
```

**Arguments**

x	An object of class <code>fars_density</code> .
time_index	Optional vector for the time axis (default is <code>1:nrow</code> ).
...	Additional arguments passed to the plot function. (ignored)

**Value**

An interactive plot of class `plotly`.

---

<code>plot.mldfm</code>	<i>Plot method for MLDFM object</i>
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---

**Description**

Dispatches to specific plot functions for factors, loadings, or residuals.

**Usage**

```
## S3 method for class 'mldfm'
plot(x, which = "factors", dates = NULL, var_names = NULL, ...)
```

**Arguments**

x	An object of class <code>mldfm</code> .
which	What to plot: one of "factors" (default), "loadings", or "residuals".
dates	Optional vector of dates (as <code>Date</code> or <code>zoo::yearqtr</code> ) to use for the x-axis. If not provided, a simple index (1:N) is used.
var_names	Optional vector of variable names to label loadings and residual axis.
...	Additional arguments (ignored)

**Value**

No return value. Called for plots generation.

---

print.fars	<i>Print method for fars object</i>
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---

**Description**

Prints a short summary of the fars object

**Usage**

```
## S3 method for class 'fars'  
print(x, ...)
```

**Arguments**

x	An object of class fars_quantiles.
...	Additional arguments (ignored).

**Value**

The input object x, returned invisibly.

---

print.fars_density	<i>Print method for fars_density objects</i>
--------------------	--

---

**Description**

Displays a brief summary of the density estimation object produced by the `density()` or `nl_density()` function.

**Usage**

```
## S3 method for class 'fars_density'  
print(x, ...)
```

**Arguments**

x	An object of class fars_density.
...	Additional arguments (ignored).

**Value**

The input object x, returned invisibly.

---

print.mldfm	<i>Print Method for MLDFM Object</i>
-------------	--------------------------------------

---

**Description**

Prints a short summary of the multilevel dynamic factor model

**Usage**

```
## S3 method for class 'mldfm'
print(x, ...)
```

**Arguments**

x	An object of class mldfm.
...	Additional arguments (ignored).

**Value**

The input object x, invisibly.

---

quantile_risk	<i>Extract Conditional Quantile from Simulated Densities</i>
---------------	--

---

**Description**

Computes the conditional quantile (e.g., 5th percentile) from a simulated skew-t distribution, generated via `density()` or `nl_density()`. The result corresponds to the risk measure (e.g., Growth-at-Risk, Inflation-at-Risk, Groth-in-Stress etc.).

**Usage**

```
quantile_risk(density, QTAU = 0.05)
```

**Arguments**

density	An object of class <code>fars_density</code> returned by <code>density()</code> or <code>nl_density()</code> .
QTAU	A numeric value between 0 and 1 indicating the quantile to extract (e.g., 0.05 for 5th percentile).

**Value**

A numeric vector of conditional quantiles (one observation for each time period).

**Examples**

```
Quantiles <- matrix(rnorm(500), ncol = 5)
fars_density <- density(Quantiles, levels = c(0.05,0.25,0.50,0.75,0.95),
est_points = 512, random_samples = 1000)
GaR <- quantile_risk(fars_density, QTAU = 0.05)
```

---

summary.fars

*Summary Method for fars Object*


---

**Description**

Prints a complete summary of the fars object.

**Usage**

```
## S3 method for class 'fars'
summary(object, ...)
```

**Arguments**

object            An object of class fars\_quantiles.  
...                Additional arguments (ignored).

**Value**

The input object object, returned invisibly.

---

summary.fars\_density    *Summary method for fars\_density objects*


---

**Description**

Provides summary statistics of the density estimation for each time observation, including the mean, median, and standard deviation of the simulated distribution.

**Usage**

```
## S3 method for class 'fars_density'
summary(object, ...)
```

**Arguments**

object            An object of class fars\_density.  
...                Additional arguments (ignored).

**Value**

A data frame with one row per time observation and columns: Observation, Mean, Median, and StdDev. The object is also printed to the console and returned invisibly.

---

`summary.mldfm`*Summary Method for MLDFM Object*

---

**Description**

Provides a complete summary of the multilevel dynamic factor model

**Usage**

```
## S3 method for class 'mldfm'  
summary(object, ...)
```

**Arguments**

`object`            An object of class `mldfm`.  
`...`             Additional arguments (ignored).

**Value**

The input object `object`, invisibly.

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