

# Package ‘KneeArrower’

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**Type** Package

**Title** Finds Cutoff Points on Knee Curves

**Version** 1.0.0

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**Description** Given a set of points around a knee curve,  
analyzes first and second derivatives to find knee points.

**License** GPL-3

**Encoding** UTF-8

**LazyData** true

**Imports** signal

**RoxygenNote** 7.1.1

**Suggests** testthat, knitr, rmarkdown

**VignetteBuilder** knitr

**NeedsCompilation** no

**Repository** CRAN

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derivative	<i>Derivative of a function with respect to x</i>
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**Description**

Derivative of a function with respect to x

**Usage**

```
derivative(x, y, m = 0, n = 50)
```

**Arguments**

x	x coordinates of points in function's domain
y	y coordinates of points in function's range
m	the order of the derivative (0 for y, 1 for y', 2 for y'')
n	number of points in the domain for interpolation

**Value**

a function representing the mth derivative of y(x) with respect to x

**Examples**

```
x <- seq(0,5,0.1)
y <- x^2 - 2*x + 3 # So dy/dx = 2x - 2
fp <- derivative(x, y, 1)
fp(2) # 2
fp(5) # 8
```

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findCutoff	<i>Finds cutoff point on knee curve</i>
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**Description**

Finds cutoff point on knee curve

**Usage**

```
findCutoff(x, y, method = "first", frac.of.steepest.slope = 0.5)
```

**Arguments**

x	vector of x coordinates of points around curve
y	vector of y coordinates of points around curve
method	the method to define the knee point. Value can be "first" for first derivative cutoff or "curvature" for maximum curvature cutoff.
frac.of.steepest.slope	the slope at the cutoff point relative to the steepest (positive or negative) slope on the curve. Only used if method is set to "first". Can be set to any number > 0 or <= 1. If the knee curve is increasing and concave down, then lower numbers will lead to higher knee points, and higher numbers will lead to lower knee points.

**Value**

a list containing the (x, y) coordinates of the knee point chosen using the specified method

**Examples**

```
# Generate some knee data
x <- runif(100, min=-3, max=3)
y <- -exp(-x) * (1+rnorm(100)/3)
plot(x, y)
# Plot knee points calculated using two different methods
points(findCutoff(x,y), col="red", pch=20, cex=3)
points(findCutoff(x,y, method="curvature"), col="blue", pch=20, cex=3)
```

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findCutoffCurvature     *Finds the point on the curve that has the maximum curvature*

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**Description**

Finds the point on the curve that has the maximum curvature

**Usage**

```
findCutoffCurvature(x, y)
```

**Arguments**

x	x coordinates of points around the curve
y	y coordinates of points around the curve

**Value**

(x, y) coordinates of the point with the greatest curvature

findCutoffFirstDerivative

*Finds the point where the derivative is a fraction of the steepest slope*

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**Description**

Finds the point where the derivative is a fraction of the steepest slope

**Usage**

```
findCutoffFirstDerivative(x, y, slope_ratio = 0.5)
```

**Arguments**

x	x coordinates of points around the curve
y	y coordinates of points around the curve
slope_ratio	the fraction of the steepest slope that defines knee point

**Value**

(x, y) coordinates of the knee point

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inverse

*Inverse of a function*

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**Description**

Inverse of a function

**Usage**

```
inverse(f, domain)
```

**Arguments**

f	univariate function
domain	domain of f given as (min, max) interval

**Value**

a function g such that  $f(x) = y$  and  $g(y) = x$

**Examples**

```
expinv <- inverse(exp, c(0,3))  
expinv(exp(1))
```

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